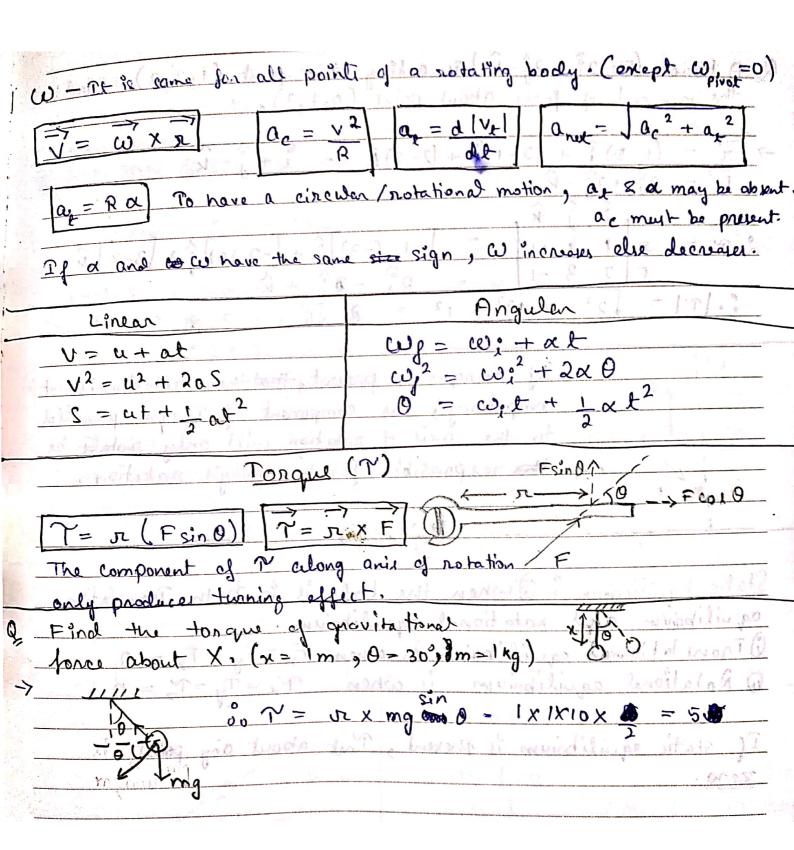
Rigid body - When	2 points in a body	y have constant olistance.
) Translation motion	81 18	
-> when two points 11		ointrol a frais
rigid body are po	•	. 11
	straight line = Rec'	tilinear
when path is a	curved line = Cu	wilinear pivol
The second of the second second		
Rotational motion	9	
> when all the part	icles (internal) ma	ve is a
circular path abo	out a lixed axis.	
The line joinging 2	internal points does n	at ramain paraellel.
	The September Course of the Se	
B) Planar motion:	A	
>	B	B = d +
	790	
A Secretaria de la composició de la comp	Plana	n Translation + notation
	X X	
Quantity	Linear	Angular
Displacement	₿ S	8
Velocity	Y	(w)
acceleration	minimum a a part	X
Fonce	F	~ (Porque)
May	What was a second with the second	I (Moment al Pinertia)
momen tum	O Set To	I (Moment of Inontia) L (Angular momentum
Billian and market of the said, market	is a table supersonal to be the time of the present of	

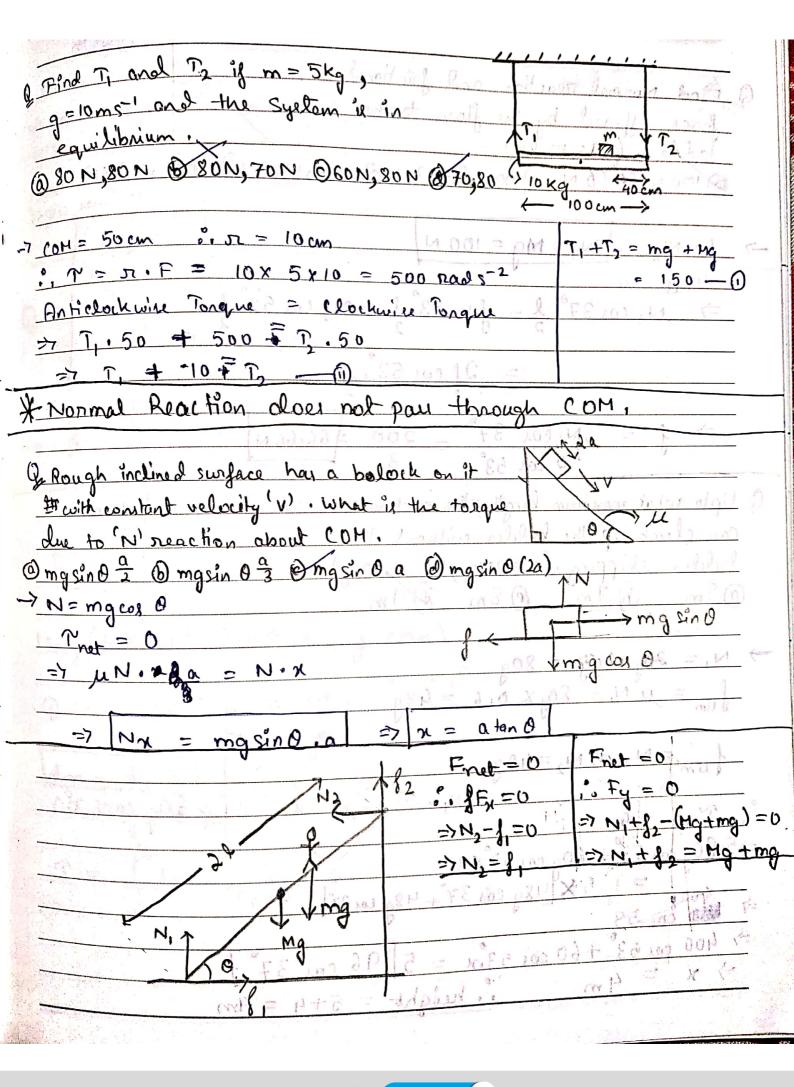


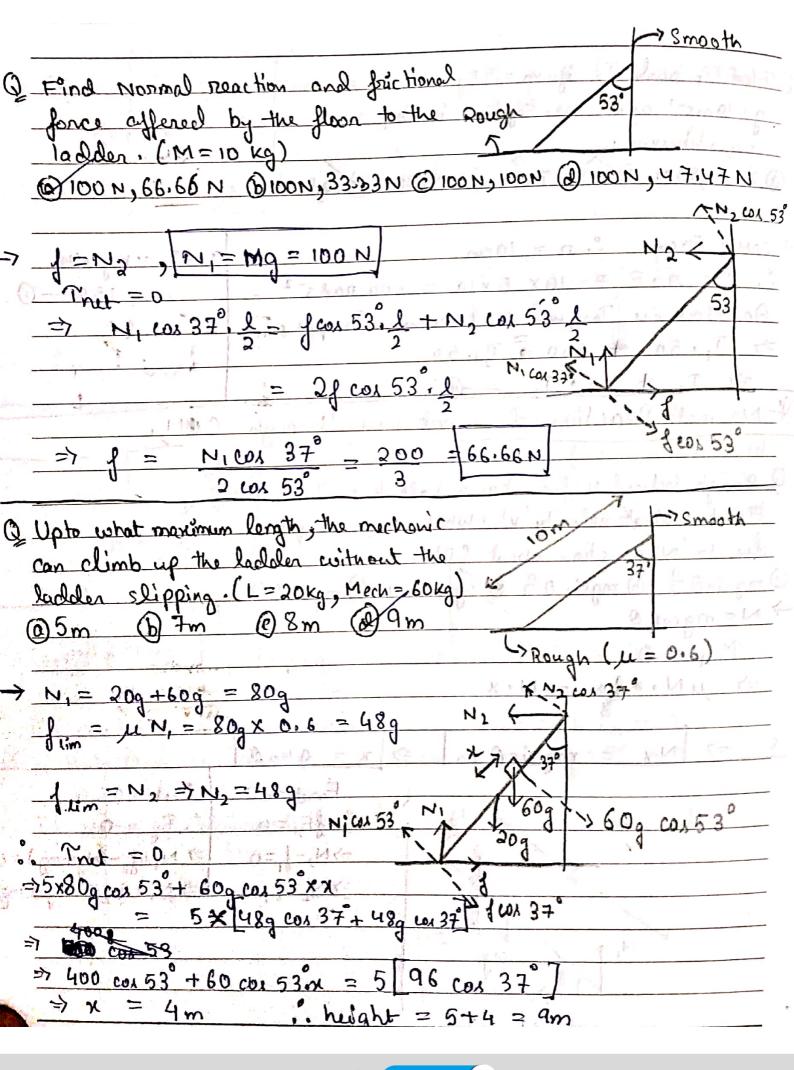
A Fonce (F=2; +3;-k) is acting at a point (1,2,92). Find the moment of force about point (0,1,3). If torque is present, that then rotation is not compulsory, The component of Torque persalled to the axis of rotation will only sotate be the responsible for the booly's notcetion. Static Equilibrium & Funen the body is in Dotn Translation

og wilibrium and notational oquilibrium.

© Trong lational equilibrium is when $F_x = F_y = F_z = 0$ © Rotational equilibrium is when $Y_x = T_y = T_z' = 0$

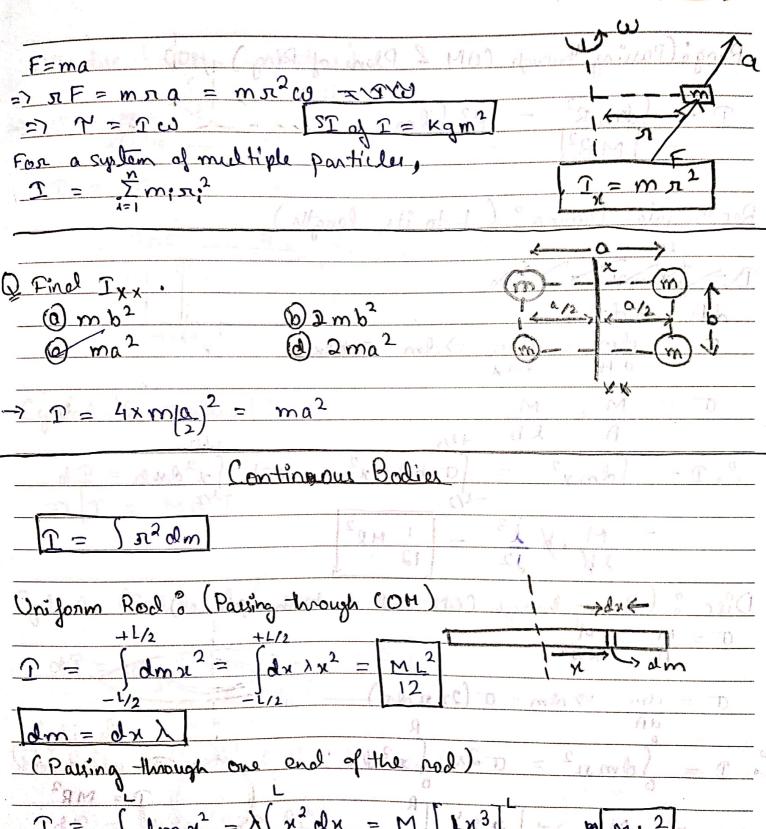
If static equilibrium is present, That about any point is

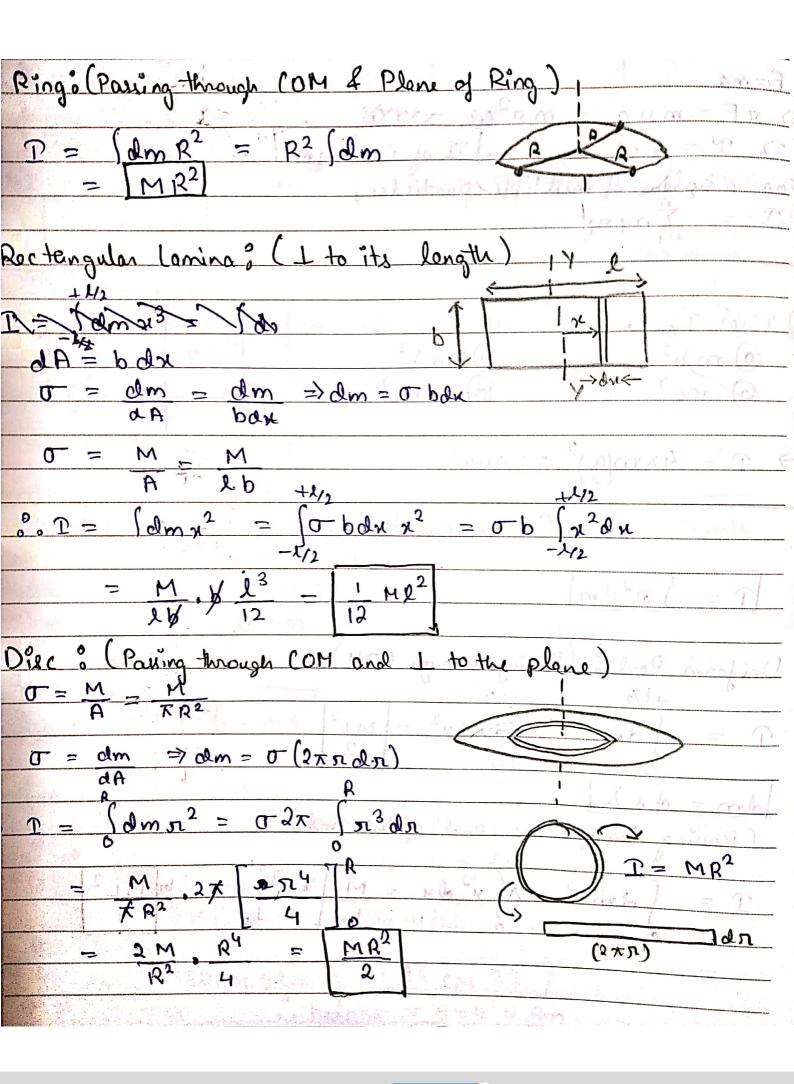


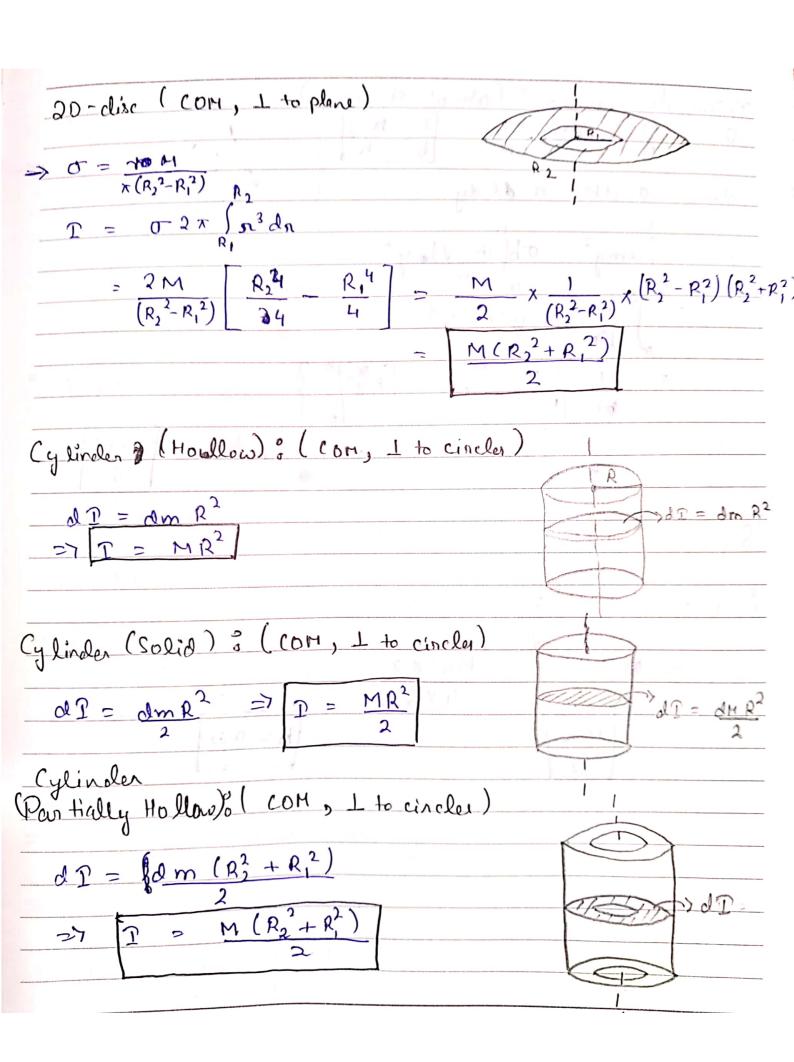


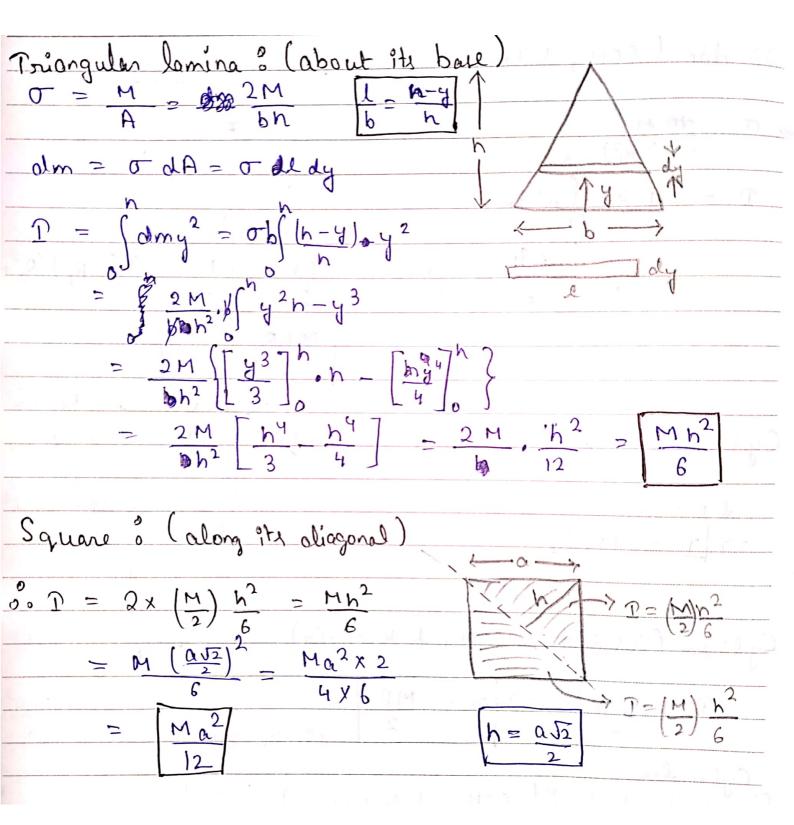
Moment of inentia

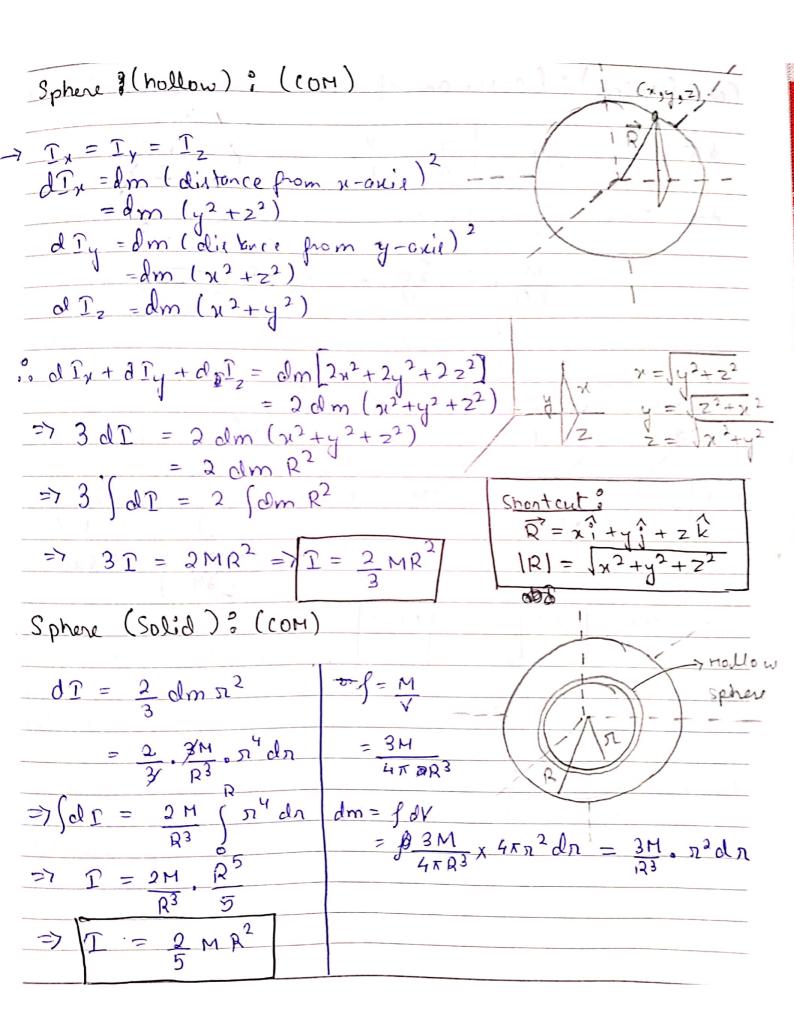


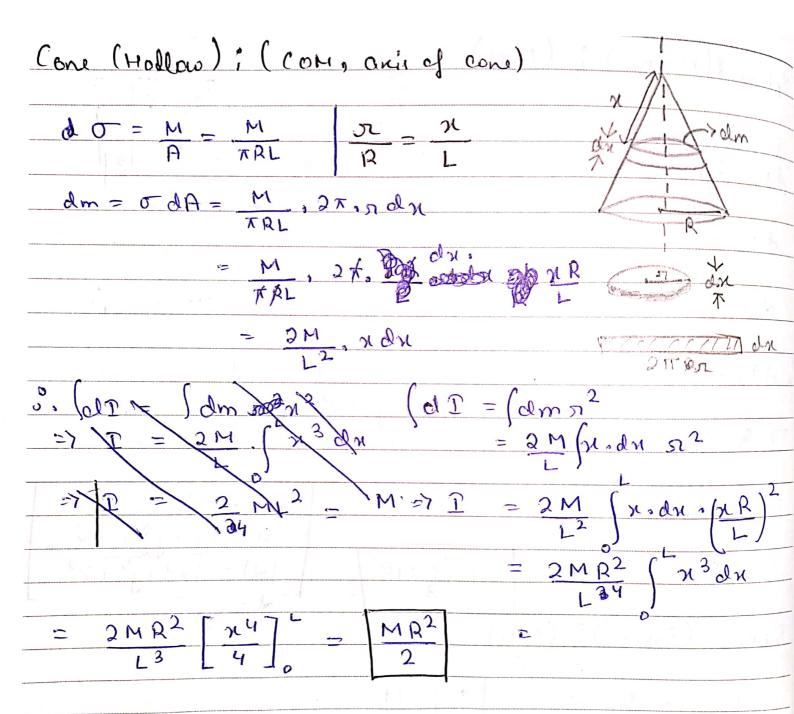












Cone (Solid)? (oxis of cone)

$$f = \frac{M}{V} = \frac{3M}{\pi R^2 n}$$

 $\oint \int dm = \int dV = \int \cdot 3\pi n^2 \cdot dn$ $= \frac{3M}{\pi n^2 n} \cdot 3\pi n^2 dn$

=
$$\frac{3M}{R^2h}$$
, $\left(\frac{xR}{h}\right)^2$. dx

 $\mathcal{R} = \int dm \, \chi^2 = \frac{3M}{R \, h^2} \int \chi^2 \, d\chi \cdot \chi^2 = \frac{3H}{R \, h^2}$

$$\int d\Omega = \int \frac{dm \, n^2}{2} \Rightarrow T = \frac{3H}{2h^3} \int n^2 \, dn \cdot dn^2 = \frac{3H}{2h^3} \cdot \frac{R^2}{h^2} \left(n^4 \, dn \right)$$

ST = X

$$= \frac{3 \text{ MR}^2}{2 \text{ h}^5} \left[\frac{15}{5} \right]^n = \frac{3 \text{ MR}^2}{10}$$

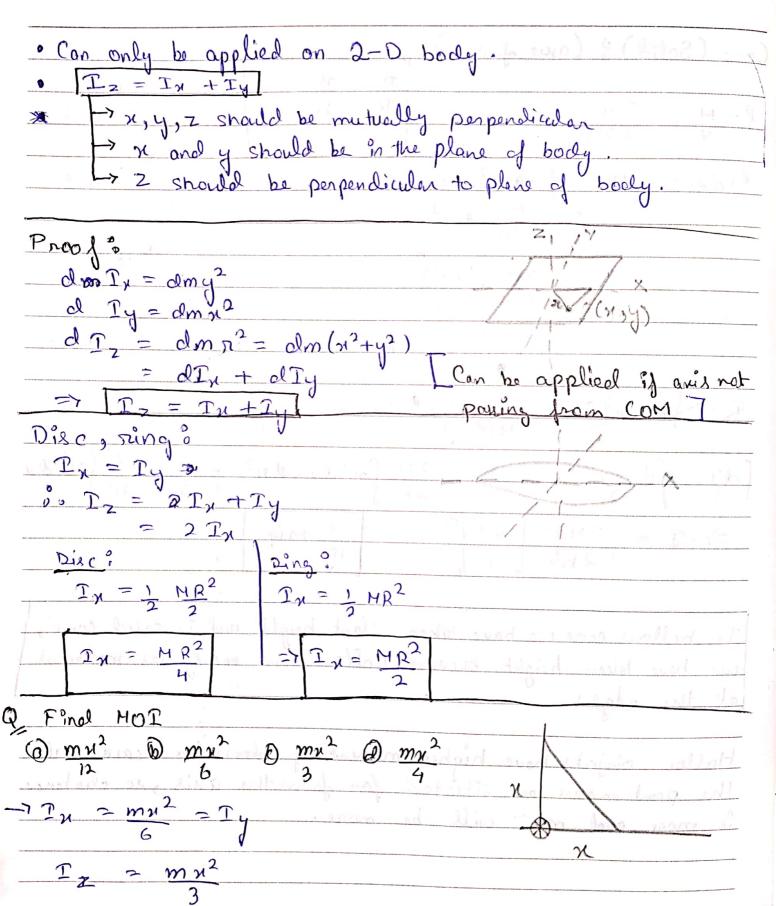
In hollow come we have taken slent height and in solid come, we have taken height because hollow come woody has material at the edge.

Hollow objects have higher moment of interinantia because all the point masses are situated for from the axis, so clistones is more and mr? will be more.





Perpendicular and axis Theorem



Parnallel axis theorem



T=
$$T_{COH} + M_{0}^{2}$$

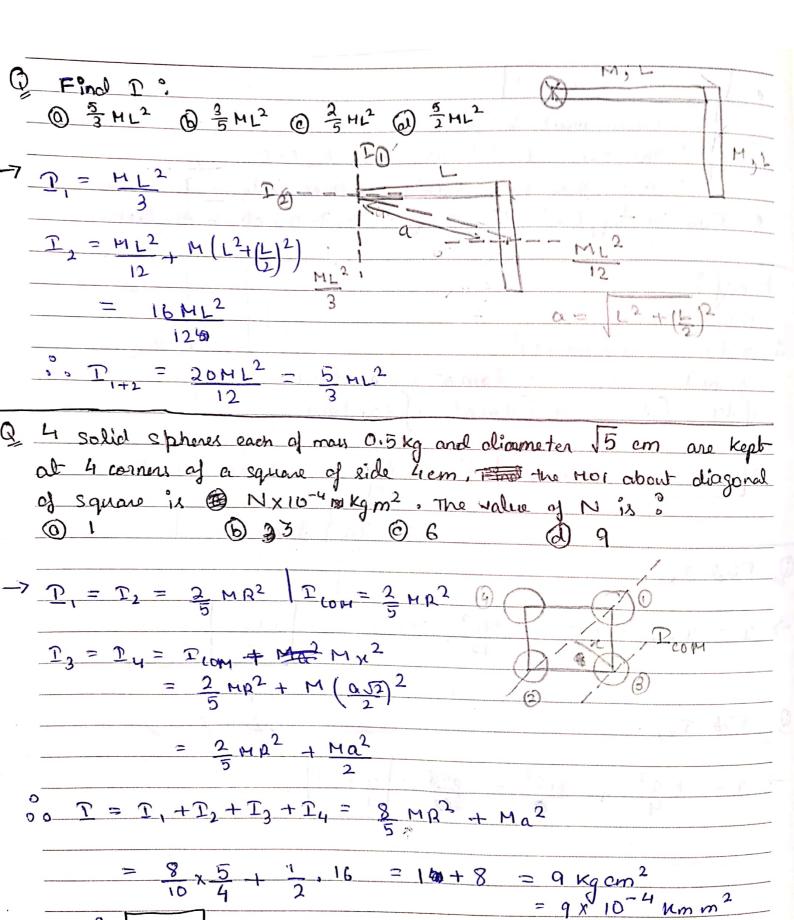
T = $T_{COH} + M_{0}^{2}$

T = $T_{COH} + M_{0}^{2}$

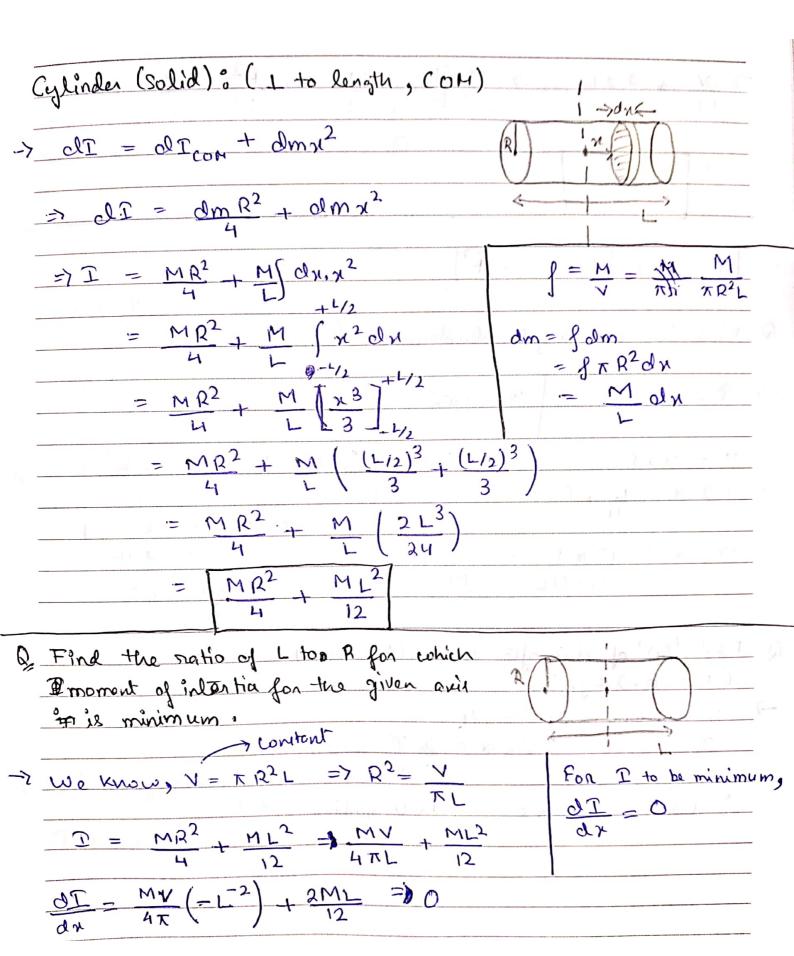
T = $T_{COH} + M_{0}^{2}$

Proof:

T = $T_{COH} + M_{0}^{2}$



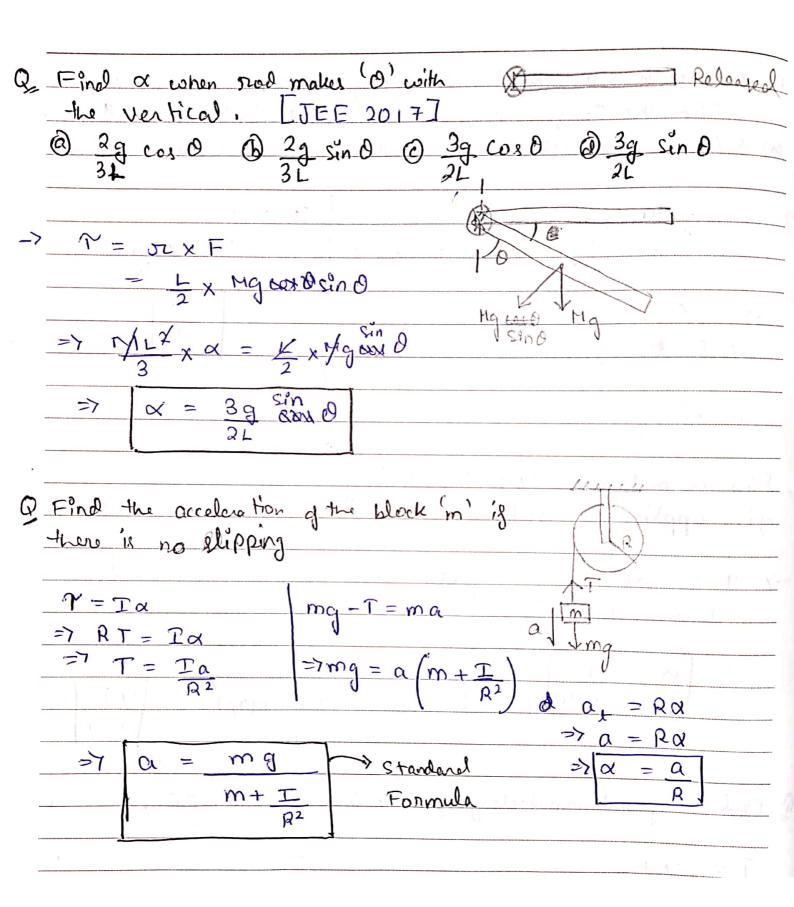
0 N = 9

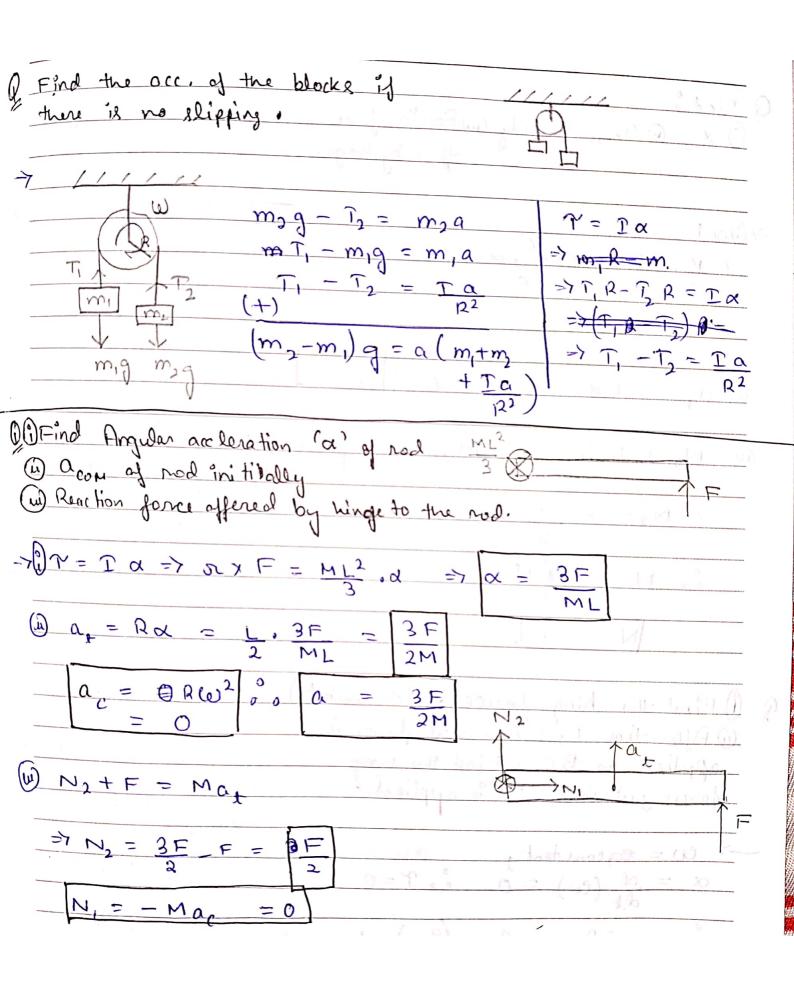


 $\Rightarrow \frac{1}{\kappa L^2} \Rightarrow \frac{1}{3} \Rightarrow \frac{1}{\kappa L^2} \Rightarrow \frac{1}{\kappa L^2$ マニュスト T = Da Q Find 'a' and angular displacement in (t) sec. K=/WK/E -7 P= 1 a 0. 0 = Wot+1xt² T= nxF => Da= LxF = 0 + 1, 3F, L² $\Rightarrow \alpha = 12 \text{ in } F = 3 F$ H, ML

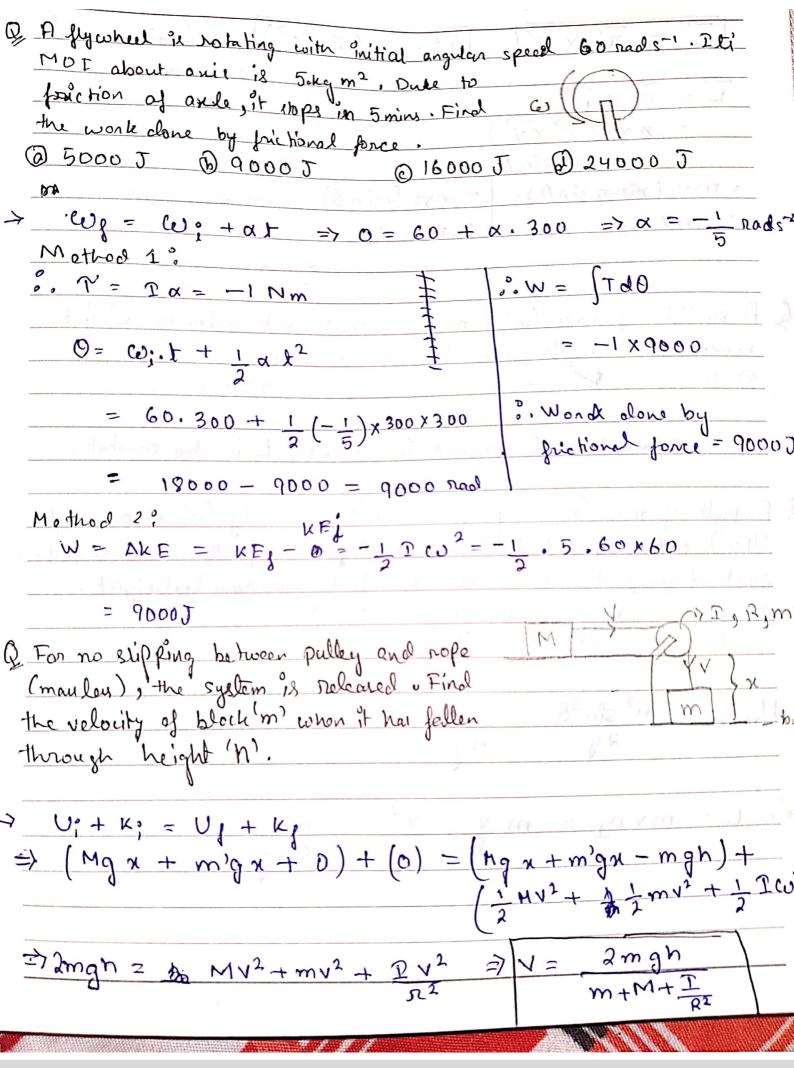
ML = 3 F. L2 Q Find (w) of olive often 5 sec.(RaR=20cm) (T = 0.2 kgm²) $-7 \gamma = 0.2 \times 20 = 4$ $T = 0.2 \quad \text{f.} \alpha = \underline{x} = 20$ 0 cu = 0 + at = 100 nadian se (3-1

Q A wheel with MOI 2 kgm² and notating at 50 pm 13 brought to rest. Find the Tonque required to bring it to rest in I min. 6) x/6 6 x/12 6 x/15 0 x/18 -> wo = 50 spm $\frac{50 \times 2\pi}{60} = \frac{5\pi}{3} \text{ accliant s}^{-1}$ x co = co + at $=700 - 5\pi + 0.60$ $\frac{7}{3} \times = -5 \times = -1$ Q Find or and a of COM immidiately often application of Force. -> イ = nxF $\Rightarrow \mathbb{T} \alpha = L \times 3F$ => | X = 9F 5ML of Find X of nod immidiately after 9t is relocated.





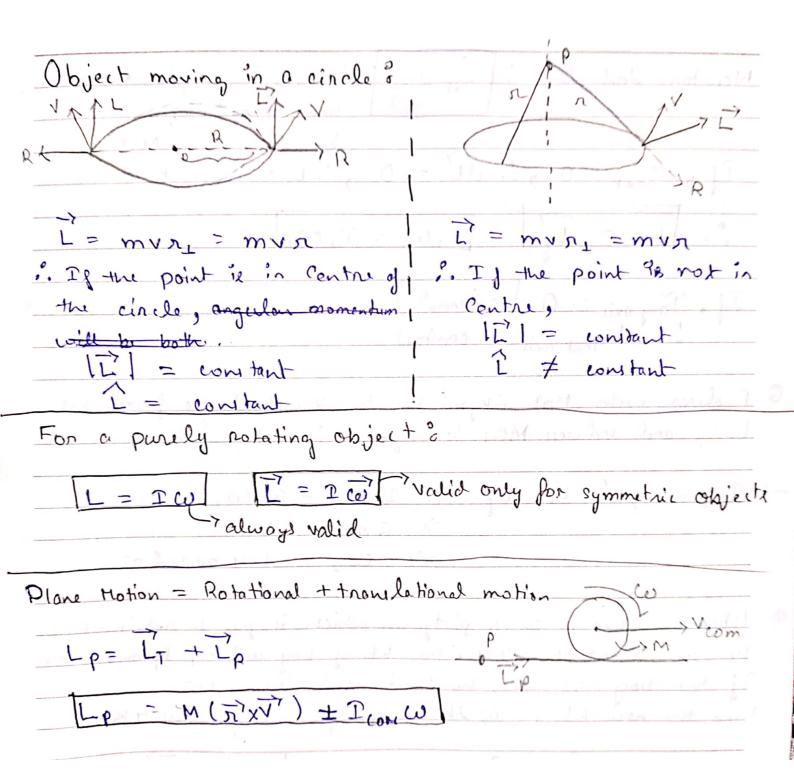
Q Find KE of lamina after 5s. (a = 10 cm = 0.1 m, m = 2 kg, 7 = 0.1 Nm) $T = \frac{Ma^2}{12} = \frac{0.1 \times 0.1 \times 2}{12 \times 00} = \frac{1}{600} \times \frac{1}{9} \text{ m}^2$ $T = T \propto \Rightarrow \propto = 60 \text{ rad s}^{-2}$ 0. No w = w + xt = 300 rad 5-1 $\frac{6. \text{ KE}}{2} = \frac{1}{2} \frac{1}{2} \frac{1}{600} \times \frac{300}{200} \times \frac{75}{200} = 75 \text{ J}$ Q A wheel I = 3kg m², T = 6Nm. Find the work clone by Tonque in 20s, @ 2400 J @ 3000 J @ 3600 J @ 1800 J $\rightarrow T = I \alpha \Rightarrow \alpha = 2 \text{ nad } s^{-2}$ we thoughth $0 = \omega_0 t + \frac{1}{2} \alpha t^2 = \frac{1}{2} \cdot 2 \cdot 20 \times 20 = 400 \text{ nadians}$.. W = STAD = 6x400 = 2400 J Wall forces = ΔKF = $KE_f - KE_{fg} = \frac{1}{2}$ A_{fg}^{2} , $CO = AA = 2 \times 20 = 40$ rads⁻¹ $K_{1} = \frac{1}{2} 2 \omega^{2} = 2400 J$ 11 W = 2400 - 0 = 2400 J

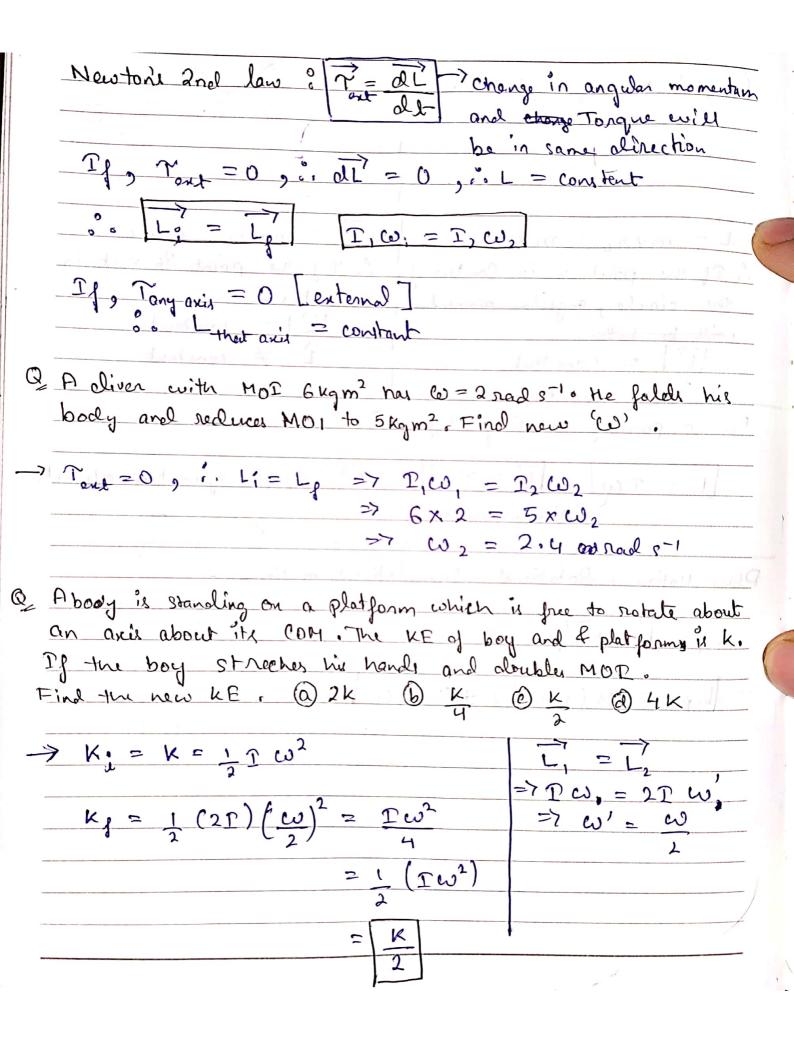




Hngular Momentum

	$[\vec{L} = \vec{\pi} \times \vec{p}] [\vec{L} = m(\vec{\pi} \times \vec{v})]$
	9
	$ \vec{\Gamma} = \vec{n} \times \vec{p} \qquad \vec{n} \times \vec{v} $ $ = m (\vec{n} \times \vec{v}) \qquad \vec{n} \times \vec{v} $ $ = m (\vec{n} \times \vec{v}) \qquad \vec{n} \times \vec{v} $
_	$= \mathbf{m} (\vec{n} \times \vec{v})$
	The state of the s
	$= m \times (x + y) = m \times (x + y)$ $= m \times (x + y)$
h	= mv2T = mv 1
	v Sin O
	Christian Chil
9	A particle of mass (m) is moving with constant velocity (v) If to
	x-axis. It's angular momentum about origin is
	60 0 Combant @ Increases (d) Decreases
	pol enola Anali. 1 OUEX OUE - /:
-7	Vis constant and raind is constant, Lie also constant.
	And Angle
Q,	A ball of man (m) is projected with velocity (v) at an angle
	(45) with neighbor to horizontal, Fingel L' of the ball w.r.t.
	point of projection when ball he at it's maximum besheight.
١.	Doint of projection when ball he at it's maximum basheight.
	Jag 2/2g 4/2g
	2 V (1) 45
	Hmax 2 12 Sin 20 = V2
_	29 49
_	
0	$\frac{1}{12} = \frac{m \sqrt{2}}{\sqrt{2}} = \frac{m \sqrt{3}}{\sqrt{2}}$
	Q 40 1.D





Q Two maces () each) are kept at O. These masses can slide on the rod radially out word. At some instant, one of the man 20 3R distance away from O, when angular velocity of system is 7 w. Find the distorce of other M at this instant > Li= Lp => PICU, = P2CO2 =7 MR2CO = [MR2+ M (3R)2+ M x2 Q When there balls love the platform , their velocity are 9 ms - each, Find the Wo of plat form when the ball leave the disc. (D) 6 rad 5-1 (D) 8 rad 5-1 @ 4 rad 5-1 -> Li=0, Tret=0, Lj=0 LP = Lf(bally) + LDisc = mVn, + Iw $\omega = -m v_{\pi_{+}} - 2 x o \cos x d$



Q Find the Cely of the System. (a) 1.33 read 5-1 (b) 4 need 6 4 news 5-1

6 3.33 sad s-1

@ 8 rool 5-1

Lo= Lg

Co; = 10 reads -1

1=0.2 m

 $L_i^2 = T \omega_i = M \Omega^2 \omega_i = \frac{50 \times (0.4)^2}{10} = 40$

L1 = (2) ring about COH of disc + D disc) cuz

= $\left[2.\left(32mn^2\right) + \frac{MR^2}{2}\right] \omega_2$

= 5 co2

 $=7 \omega_2 = \frac{40}{5} = 8$

Q Boy is standing on a patplet form which is free to notate, holding an umbrella.

If umbrella is twisted with angular speal

of 2 rads -1 with respect to platform.

Find Copplatform final. IBTP = 3 × 10-3, Pu = 2× 10-3

@ 1.33 Do.u

-> L; = L g=0 , COUP = OUG - COPG = WOG - (-W)

=> 2 = Coun + co

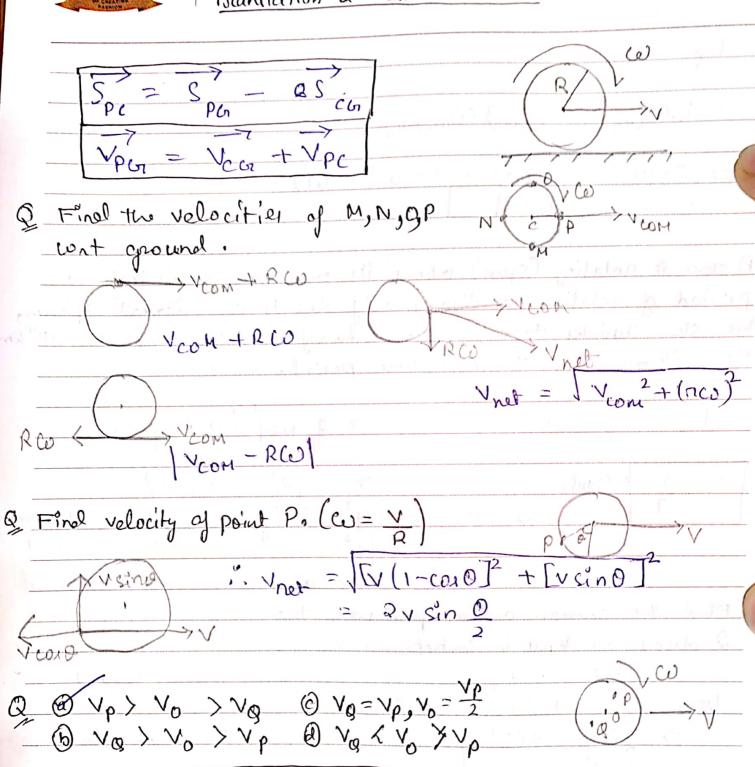
=> COUG = 2 - CO

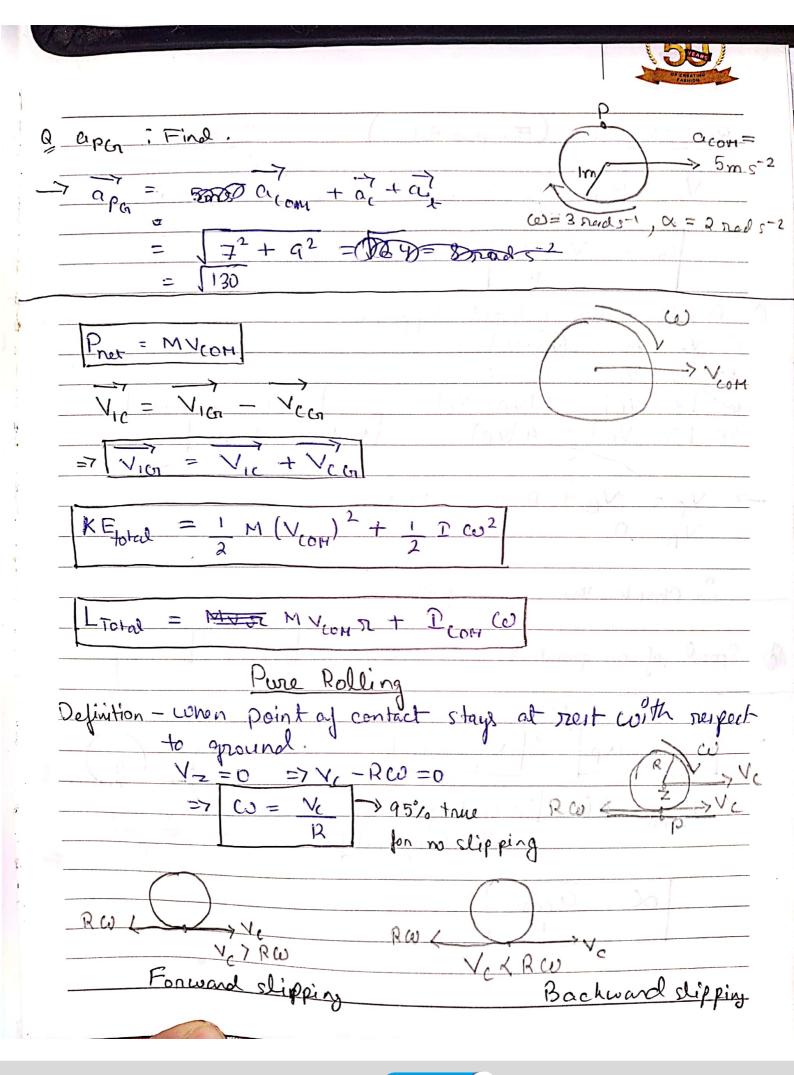
00 Le = 0 => I (CO UC) + I (P+B) $\Rightarrow 2 \times 10^{-3} \times (2 - 0) + 3 \times 10^{-3} (-0) = 0$ =7 $CO = \frac{4}{5} = 0.8$ a A stan is notating (spin) about its own axis such that its period of notation is 30 days. If due to on interval explain, the stan shrinks to nebula stan (dwarf stan) such that R; = 104 km Rg = 3km, Final the new time period. - Li=Lg =7 I, W,=I, W, =7 2 HR; = 2 HR, 2 W2 $\frac{7}{7} \cos_{1} R_{1}^{2} = \cos_{2} R_{2}^{2}$ $= 7 R_{2}^{2} - R_{1}^{2} = 7 T_{3}^{2} = R_{2}^{2} T_{1}^{2} - 9 x_{20}^{2} + 2 x_{20}^{2} + 2$ = 2332,85 Q Final the common angular speed when the 2 disce one seput in contact 1 2 2 W + 2 T W = 3 T W)

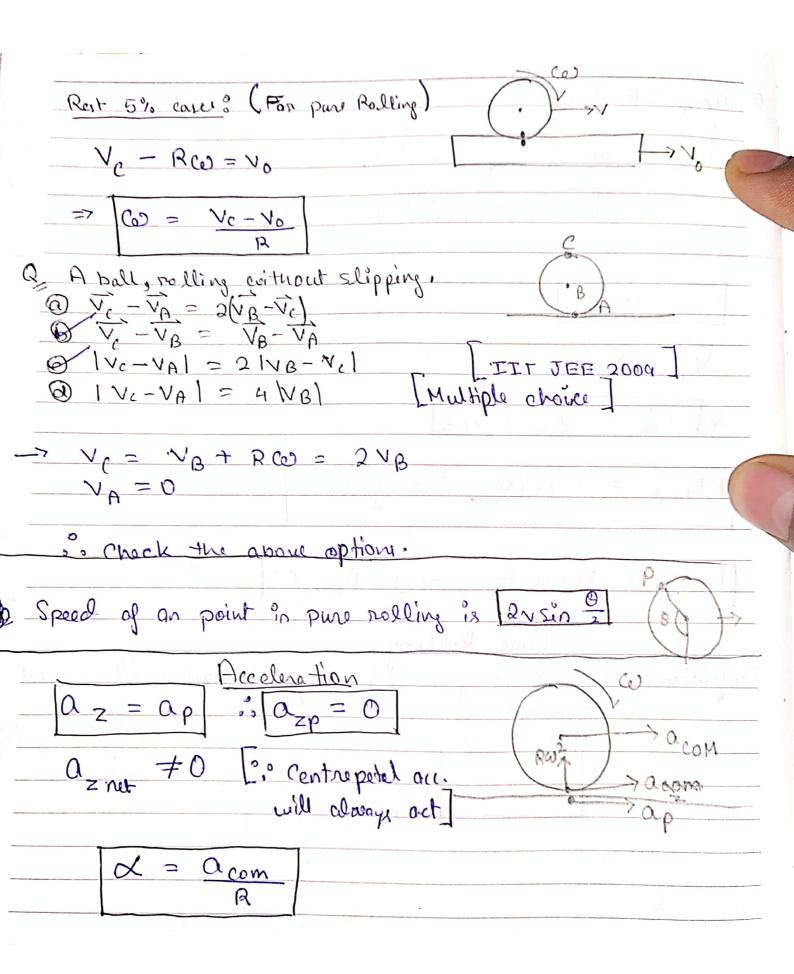
>> 4co = 3co)



Translation a+ Cincular motion







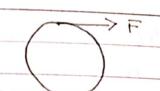
Exiction produces initial torque for the body to start rolling, after some historiale, tangential velocity decreases, angular velocity Increases after some time, tangential valority will be equal to arongular velocity, then pure rolling will start, then friction will cease to act. QAdisc (M, R) Starts rolling on a surface with coefficient of friction (le) what will be the targential velocity of COM after the body Starte pure rolling. (0);=0, (0) = (0) -> f= uMg, ag=-lig N= No-(ug) + Putting 10 in 10 9 = V0 - V



Forces in Pure Rolling

Addin (1) and (11),
$$\alpha = \frac{20}{70}$$
, $\beta = \frac{30}{70}$ $\beta = \frac{30}{70}$

Q Sold sphere, (M,A), a = ?.



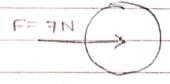
$$afF = Ma - 0$$

$$FR - fR = \frac{2}{5}MR^2 \alpha = \frac{2}{5}MR^2 \cdot \frac{\alpha}{R}$$

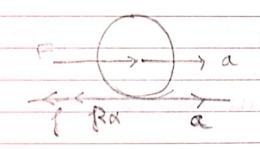
Adding (1), (1), 2F = 7Ma

=> F-J = = Ma -0

Q Solid Sphere,

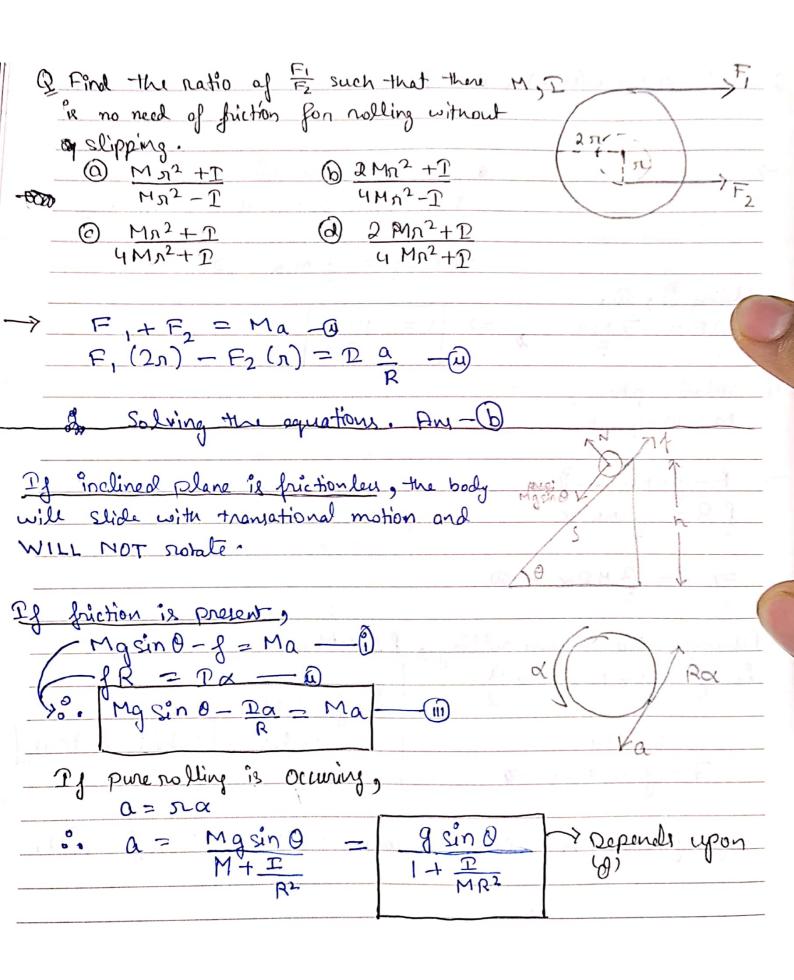


7 F-1=Ma -Q (R = 2 MR2 X



Assuming this is pure rolling , of & MMg

$$\int = \frac{2}{5} \times 10 \times 2 \times \frac{Q}{2}$$



Q what would be the velocity of the body at the bottom ? $\Rightarrow \sqrt{2} = 0 + 2 \cdot \left(\frac{q \sin \theta}{1 + \frac{\Gamma}{H R^2}}\right) \times \frac{h}{\sin \theta}$ -> y2= u2 +2as $\sin \theta = \frac{h}{c}$ $= \frac{29h}{1+\frac{T}{MR^2}}$ Does not depend upon θ' . Freq & Stim Note - State fraction is present. From (), f = Mgsin 0 - no Ma =7 $\int_{\text{Static}} = Mq \sin \theta \left(\frac{T}{MR^2 + T} \right)$ Work done by piction = 0 $W_{F \rightarrow 7} = W_{F \rightarrow R}$ Crequired Priction Conservation of ME is valid in pure rolling. I 2 solid cylindere P and a of same may and same rading Start rolling down a fixed inclined plane on a fixed height on at a fixed time. Cylinder P has most of its man concentrated or on its en surface while Q have & most of the man conce concentrated on its axis. Which of the following statements @ Both PRQ reach ground simultaneowsly. (b) P how larger linear acceleration. (a) Both reach with same translational kinetic energy on ground. (1) (1) reaches ground with more angular speed.